

## Try These

1. If a person has three times as many quarters as dimes and the total amount of money is \$5.95, find the number of quarters and dimes.
2. A pile of 18 coins consists of pennies and nickels. If the total amount of the coins is  $38\epsilon$ , find the number of pennies and nickels.
3. A small child has 6 more quarters than nickels. If the total amount of the coins is \$3.00, find the number of nickels and quarters the child has.
4. A child's bank contains 32 coins consisting of nickels and quarters. If the total amount of money is \$3.80, find the number of nickels and quarters in the bank.
5. A person has twice as many dimes as she has pennies and three more nickels than pennies. If the total amount of the coins is \$1.97, find the numbers of each type of coin the person has.
6. In a bank, there are three times as many quarters as half dollars and 6 more dimes than half dollars. If the total amount of the money in the bank is \$4.65, find the number of each type of coin in the bank.
7. A person bought 12 stamps consisting of  $37\epsilon$  stamps and  $23\epsilon$  stamps. If the cost of the stamps is \$3.74, find the number of each type of the stamps purchased.
8. A dairy store sold a total of 80 ice cream sandwiches and ice cream bars. If the sandwiches cost \$0.69 each and the bars cost \$0.75 each and the store made \$58.08, find the number of each sold.
9. An office supply store sells college-ruled notebook paper for \$1.59 a ream and wide-ruled notebook paper for \$2.29 a ream. If a student purchased 9 reams of notebook paper and paid \$15.71, how many reams of each type of paper did the student purchase?
10. A clerk is given \$75 in bills to put in a cash drawer at the start of a workday. There are twice as many \$1 bills as \$5 bills and one less \$10 bill than \$5 bills. How many of each type of bill are there?

## LESSON 11 Solving Coin Problems

### SOLUTIONS:

1. Let  $x$  = the number of dimes and  $3x$  = the number of quarters; then the value of the dimes is  $10x$  and the value of the quarters is  $25 \cdot 3x$  or  $75x$ .

$$10x + 25 \cdot 3x = 5.95 \times 100$$

$$10x + 75x = 595$$

$$85x = 595$$

$$\frac{85^1 x}{85^1} = \frac{595}{85}$$

$$x = 7 \text{ dimes}$$

$$3x = 3 \cdot 7 = 21 \text{ quarters}$$

2. Let  $x$  = the number of nickels and  $18 - x$  = the number of pennies; then the value of the nickels is  $5x$  and the value of the pennies is  $1 \cdot (18 - x)$ .

$$5x + 18 - x = 38$$

$$4x + 18 = 38$$

$$4x + 18 - 18 = 38 - 18$$

$$4x = 20$$

$$\frac{4^1 x}{4^1} = \frac{20}{4}$$

$$x = 5 \text{ nickels}$$

$$18 - x = 18 - 5 = 13 \text{ pennies}$$

3. Let  $x$  = the number of nickels and  $x + 6$  = the number of quarters; then the value of the nickels is  $5x$  and the value of the quarters is  $25(x + 6)$ .

$$5x + 25(x + 6) = 3 \times 100$$

$$5x + 25x + 150 = 300$$

$$30x + 150 = 300$$

$$30x + 150 - 150 = 300 - 150$$

$$30x = 150$$

$$\frac{30^1 x}{30^1} = \frac{150}{30}$$

$$x = 5 \text{ nickels}$$

$$x + 6 = 5 + 6 = 11 \text{ quarters}$$

4. Let  $x$  = the number of quarters and  $32 - x$  = the number of nickels; then the value of the quarters is  $25x$  and the value of the nickels is  $5(32 - x)$ .

$$25x + 5(32 - x) = 3.80 \times 100$$

$$25x + 160 - 5x = 380$$

$$20x + 160 = 380$$

$$20x + 160 - 160 = 380 - 160$$

$$20x = 220$$

$$\frac{20^1 x}{20^1} = \frac{220}{20}$$

$$x = 11 \text{ quarters}$$

$$32 - x = 32 - 11 = 21 \text{ nickels}$$

5. Let  $x$  = the number of pennies,  $2x$  = the number of dimes, and  $x + 3$  = the number of nickels; then the value of the pennies is  $1x$ , the value of the dimes is  $10 \cdot 2x$ , and the value of the nickels is  $5(x + 3)$ .

$$x + 10 \cdot 2x + 5(x + 3) = 1.97 \times 100$$

$$x + 20x + 5x + 15 = 197$$

$$26x + 15 = 197$$

$$26x + 15 - 15 = 197 - 15$$

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$$26x = 182$$

$$\frac{26^1 x}{26^1} = \frac{182}{26}$$

$$x = 7 \text{ pennies}$$

$$2x = 2 \cdot 7 = 14 \text{ dimes}$$

$$x + 3 = 7 + 3 = 10 \text{ nickels}$$

6. Let  $x$  = the number of half dollars,  $3x$  = the number of quarters, and  $x + 6$  = the number of dimes; then the value of the half dollars is  $50x$ , the value of the quarters is  $25 \cdot 3x$ , and the value of the dimes is  $10(x + 6)$ .

$$50x + 25 \cdot 3x + 10(x + 6) = 4.65 \times 100$$

$$50x + 75x + 10x + 60 = 465$$

$$135x + 60 = 465$$

$$135x + 60 - 60 = 465 - 60$$

$$135x = 405$$

$$\frac{135^1 x}{135^1} = \frac{405}{135}$$

$$x = 3 \text{ half dollars}$$

$$3x = 3 \cdot 3 = 9 \text{ quarters}$$

$$x + 6 = 3 + 6 = 9 \text{ dimes}$$

7. Let  $x$  = the number of  $37\epsilon$  stamps and  $(12 - x)$  = the number of  $23\epsilon$  stamps; then the value of the  $37\epsilon$  stamps is  $37x$  and the value of the  $23\epsilon$  stamps is  $23(12 - x)$ .

$$37x + 23(12 - x) = 3.74 \times 100$$

$$37x + 276 - 23x = 374$$

$$14x + 276 = 374$$

$$14x + 276 - 276 = 374 - 276$$

$$14x = 98$$

$$\frac{14^1 x}{14^1} = \frac{98}{14}$$

$$x = 7 \quad 37\text{¢ stamps}$$

$$12 - x = 12 - 7 = 5 \quad 23\text{¢ stamps}$$

8. Let  $x$  = the number of sandwiches and  $(80 - x)$  = the number of bars; then the cost of the sandwiches is  $69x$  and the cost of the bars is  $75(80 - x)$ .

$$69x + 75(80 - x) = 5808$$

$$69x + 6000 - 75x = 5808$$

$$6000 - 6x = 5808$$

$$6000 - 6000 - 6x = 5808 - 6000$$

$$-6x = -192$$

$$\frac{-6^1 x}{-6^1} = \frac{-192}{-6}$$

$$x = 32 \text{ sandwiches}$$

$$80 - x = 80 - 32 = 48 \text{ bars}$$

9. Let  $x$  = the number of reams of college-ruled paper and  $9 - x$  = the number of reams of wide-ruled paper; then the cost of the college-ruled paper is  $159x$  and the cost of the wide-ruled paper is  $229(9 - x)$ .

$$159x + 229(9 - x) = 1571$$

$$159x + 2061 - 229x = 1571$$

$$-70x + 2061 = 1571$$

$$-70x + 2061 - 2061 = 1571 - 2061$$

## LESSON 11 Solving Coin Problems

$$-70x = -490$$

$$\frac{-70^1 x}{-70^1} = \frac{-490}{-70}$$

$$x = 7 \text{ reams of college-ruled paper}$$

$$9 - x = 9 - 7 = 2 \text{ reams of wide-ruled paper}$$

10. Let  $x$  = the number of \$5 bills,  $2x$  = the number of \$1 bills, and  $x - 1$  = the number of \$10 bills; then the value of the \$5 bills is  $5x$ , the value of the \$1 bills is  $1 \cdot 2x$ , and the value of the \$10 bills is  $10(x - 1)$ .

$$5x + 2x + 10(x - 1) = 75$$

$$5x + 2x + 10x - 10 = 75$$

$$17x - 10 = 75$$

$$17x - 10 + 10 = 75 + 10$$

$$17x = 85$$

$$\frac{17^1 x}{17^1} = \frac{85}{17}$$

$$x = 5 \text{ five-dollar bills}$$

$$2x = 2 \cdot 5 = 10 \text{ one-dollar bills}$$

$$x - 1 = 5 - 1 = 4 \text{ ten-dollar bills}$$